

Digital Control Systems

Time: 3 hours

Max. Marks: 70

Note: Answer ALL questions in Part-A and any FIVE questions from Part-B
Part-A (10 X 2=20 Marks)

- Find the inverse z-transform of $\frac{10z}{(z-1)(z-2)}$.
- What are the different types of sampling operations?
- Describe the principle of pulse transfer function.
- State Complex differentiation and Partial differentiation theorem.
- Write the stability conditions in the z-plane.
- Define asymptotic stability.
- What is cascade compensation?
- What is the information that can be obtained from frequency response plots?
- Write the state feedback control law.
- How to determine the marginal stability using Jury method?

Part- B (5 X 10 = 50 Marks)

- (a) With the help of suitable circuit explain the principle of operation of sample and hold devices. Derive the transfer function of zero order hold circuit. (6)
(b) Calculate the inverse z-transform of following transfer function (4)

$$X(z) = \frac{z^2}{(z-1)^2(z-e^{-at})}$$

- (a) Explain the mapping between S-plane and Z-plane with primary strips and complementary strips. (5)
(b) For the sampled data system of fig.1, find the response to unit step input, given

$$G(s) = \frac{1}{s+1}. \quad (5)$$

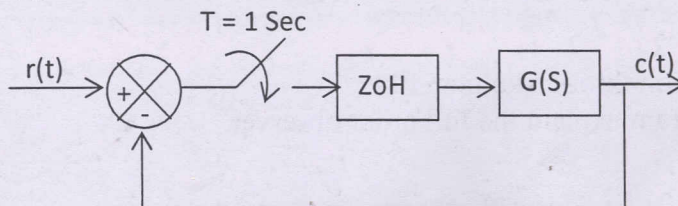


Figure:1

13. (a) Find the state transition matrix and write its properties. (4)

(b) Determine the state controllability and observability of the system described by

$$\begin{bmatrix} \frac{dx_1}{dt} \\ \frac{dx_2}{dt} \\ \frac{dx_3}{dt} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t)$$

$$y = \begin{bmatrix} 4 & 5 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad (6)$$

14. (a) Discuss Liapunov stability analysis for discrete time system. (4)

(b) Determine the stability of the equilibrium state for the system defined by the equations.

$$\begin{aligned} x_1(k+1) &= x_2(k) + 0.2x_2(k) + 0.4 \\ x_2(k+1) &= 0.5x_1(k) - 0.5 \end{aligned} \quad (6)$$

15. A block diagram of a digital control system is shown in Fig. 2. Design a PID controller to eliminate the steady-state error due to a step input and simultaneously realizing a good transient response, and the ramp-error constant K_V should equal 5. The controlled process is represented by the transfer function $G_p(s) = \frac{10}{(s+1)(s+2)}$ and $T = 0.1$ Sec. (10)

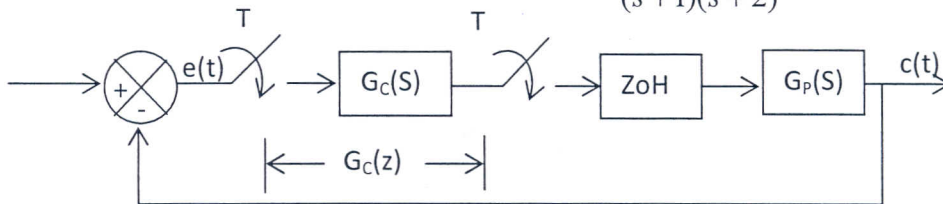


Figure:2

16. A discrete time regulator system has the plant equation (10)

$$X(k+1) = \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix} X(k) + \begin{bmatrix} 4 \\ 3 \end{bmatrix} u(k)$$

$$y(k) = \begin{bmatrix} 1 & 1 \end{bmatrix} X(k) + 7u(k)$$

Design a state feedback control algorithm with $u(k) = -Kx(k)$ which places the closed loop characteristic roots at $+j\frac{1}{2}, -j\frac{1}{2}$.

17. (a) Explain state estimation through kalman filter (6)

(b) With neat block diagram explain the full order observer. (4)